

## This Week / Next Week

- Warmups #1 and #2a/2b for this week
  - due by 10 AM before Weds. class and Fri. class this week
  - after that, due by 10 AM before Mon. or Weds. class
- Homework #1 opened today
  - it is due on Sunday night (11:59 pm)
  - after that, we move to due dates on Wednesday and Sunday
- Quiz #1
  - our first 20-minute quiz will be NEXT Friday (not this week!)
- Help Sessions
  - first one is with me on Weds. evening (8-10 pm)
  - here is the Zoom link: <https://zoom.us/j/2897909637>  
(passcode: 10112)

1

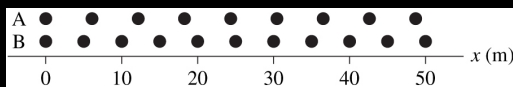
## Velocity

PHYS 20, Chap. 26, Pg 2

2

### ConcepTest 1 Motion Diagrams

Two runners jog along a track. The positions are shown at 1 s time intervals. Which runner is moving faster?



1. runner A
2. runner B
3. both the same

$$v = \frac{\Delta x}{\Delta t}$$

**Follow-up:** What are the speeds of the runners?

0 of 5

PHYS 11, Chap. 1, Pg 3

3

A bird flies a distance of 3 m in only 1/3 second.

- 1) What does the ratio  $3/(1/3)$  tell you?
- 2) What does the ratio  $(1/3)/3$  tell you?
- 3) How far would the bird fly in 1/10 second?
- 4) How long does it take the bird to fly 4 m?

1.12

PHYS 11: Chap. 1, Pg 4

4

How many paces is it (in a straight line) between Washington and Los Angeles?

~3000 miles

~ $7.5 \times 10^6$  paces

How long would it take you to walk that distance (assuming no stops at all)?

~ $7.5 \times 10^6$  secs ~ 2000 hrs ~ 80 days

Google Maps  
2700 miles  
860 hrs

PHYS 11: Chap. 1, Pg 5

5

## Chapter 2 – Kinematics in One Dimension

- Graphical representations of motion
- Uniform motion
- Instantaneous velocity
- Acceleration
- Motion with constant acceleration
  - ✓ solving 1D motion problems
  - ✓ free fall
  - ✓ motion on an inclined plane

PHYS 20, Chap. 26, Pg 5

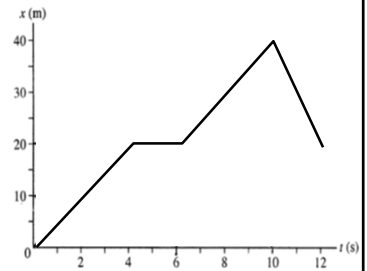
6

## Graphical Representations

PHYS 22: Chap. 26, Pg 7

7

This  $x$  vs.  $t$  graph shows the position of an object moving in a straight line for 12 seconds.



- 1) Find the position of the object at  $t = 2$ ,  $t = 6$ ,  $t = 10$ .
- 2) Find the velocity of the object during each stage.

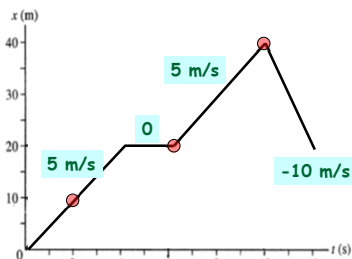
2.1

PHYS 22: Chap. 26, Pg 8

8

This  $x$  vs.  $t$  graph shows the position of an object moving in a straight line for 12 seconds.

$$v = \frac{\Delta x}{\Delta t}$$



- 1) Find the position of the object at  $t = 2$ ,  $t = 6$ ,  $t = 10$ .
- 2) Find the velocity of the object during each stage.

2.1

PHYS 22: Chap. 26, Pg 9

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### TACTICS BOX 2.1 Interpreting position-versus-time graphs



Information about motion can be obtained from position-versus-time graphs as follows:

- 1 Determine an object's *position* at time  $t$  by reading the graph at that instant of time.
- 2 Determine the object's *velocity* at time  $t$  by finding the *slope* of the position graph at that point. Steeper slopes correspond to faster speeds.
- 3 Determine the *direction of motion* by noting the *sign of the slope*. Positive slopes correspond to positive velocities and, hence, to motion to the right (or up). Negative slopes correspond to negative velocities and, hence, to motion to the left (or down).

Exercises 2,3

PHYS 22: Chap. 2, Pg 10

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## Let's check...

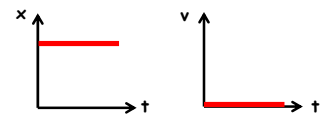
- 1) Draw  $x$  vs.  $t$  and  $v$  vs.  $t$  graphs for an object at rest at  $x = 5$  m.
- 2) Draw  $x$  vs.  $t$  and  $v$  vs.  $t$  graphs for an object moving at a constant velocity of  $+3$  m/s.
- 3) Draw #2 again, but for a velocity of  $-10$  m/s.

2.5

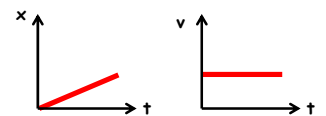
PHYS 11: Chap. 2, Pg 11

11

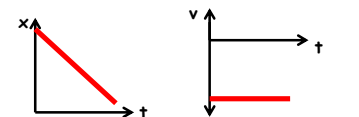
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- 3) Draw #2 again, but for a velocity of  $-10$  m/s.



2.5

PHYS 11: Chap. 2, Pg 12

12

Sketch  $x$  vs.  $t$  graphs for the following motions. Include numerical scales on the axes with units that are reasonable for this motion.

1) A student walks to the bus stop, waits for the bus, then rides to campus. Assume the motion is along a straight street.

2) A student walks slowly to the bus stop, realizes that he forgot his homework, and quickly walks back home to retrieve it.

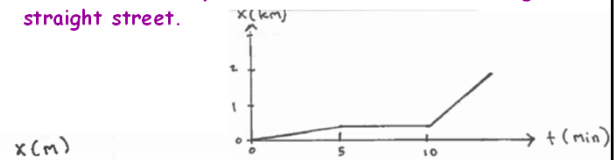
3) A quarterback drops back 10 yards from the line of scrimmage, then throws a 20 yard pass to the tight end, who catches it and sprints 20 yards to the goal line. Draw the graph for the football.

1.32 PHYS 21: Chap. 2, Pg 13

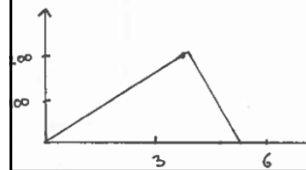
13

Sketch  $x$  vs.  $t$  graphs for the following motions. Include numerical scales with reasonable units.

1) A student walks to the bus stop, waits for the bus, then rides to campus. Assume the motion is along a straight street.



2) A student walks slowly to the bus stop, realizes that he forgot his homework, and quickly walks back home to retrieve it.

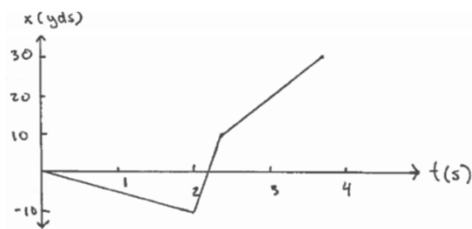


PHYS 11: Chap. 2, Pg 14

14

Sketch  $x$  vs.  $t$  graphs for the following motions. Include numerical scales on the axes with units that are reasonable for this motion.

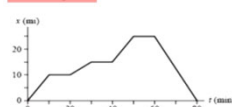
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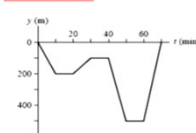
1.32 PHYS 11: Chap. 2, Pg 15

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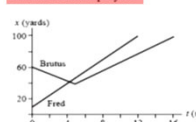
a. Moving car



b. Submarine



c. Two football players



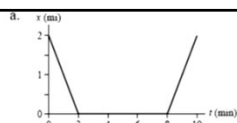
Write a short story about what is happening in the  $x$  vs.  $t$  graphs shown.

Be creative, with real characters and situations.

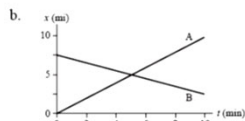
Note the distances moved and the times elapsed, including velocities, etc.

1.33 PHYS 21: Chap. 2, Pg 16

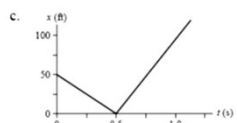
16



Tell a short story about what is happening in the  $x$  vs.  $t$  graphs shown.



You should specifically refer to the speeds of the objects in your story.



2.3 PHYS 21: Chap. 2, Pg 17

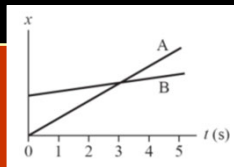
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### ConceptTest 3

### Speed and Position

At time  $t = 1$  s, how does the speed of object A compare to that of object B?

1.  $v_A > v_B$
2.  $v_A = v_B$
3.  $v_A < v_B$



Follow-up: Do objects A and B ever have the same speed? When?

0 of 5

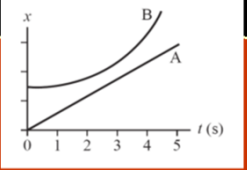
PHYS 21: Chap. 2, Pg 18

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**ConceptTest 4 Speed and Position**

At time  $t = 1$  s, how does the speed of object A compare to that of object B?

1.  $v_A > v_B$
2.  $v_A = v_B$
3.  $v_A < v_B$



**Follow-up:** Do objects A and B ever have the same speed? When?

0 of 5

PHYS 21: Chap. 2, Pg 18

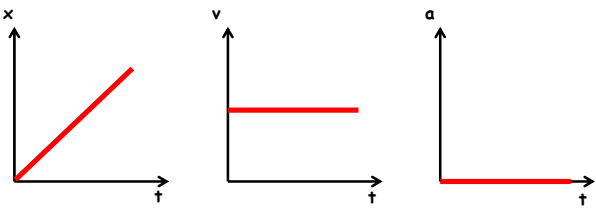
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**Velocity and Acceleration**

PHYS 21: Chap. 2, Pg 20

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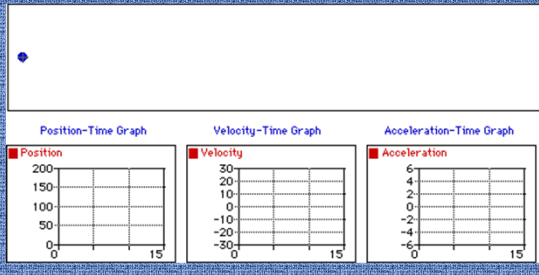
Draw the following graphs (position, velocity, acceleration) for an object that is moving at **constant velocity** (starting with  $v = v_0$  at  $x = 0$ ).



PHYS 21: Chap. 2, Pg 21

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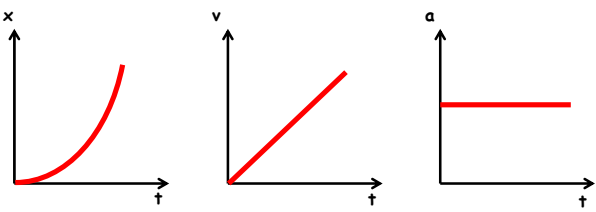
**Motion Diagrams and Graphs**  
**constant velocity**



PHYS 21: Chap. 2, Pg 22

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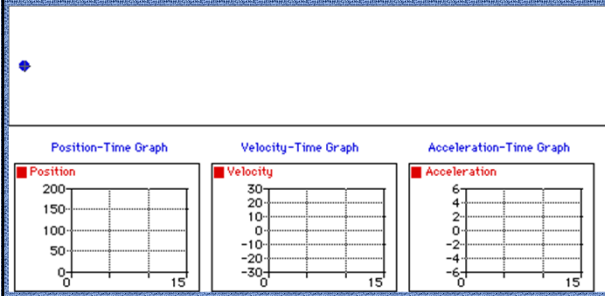
Draw the following graphs (position, velocity, acceleration) for an object that is moving with a **constant positive acceleration** (starting with  $v = 0$  at  $x = 0$ ).



PHYS 21: Chap. 2, Pg 23

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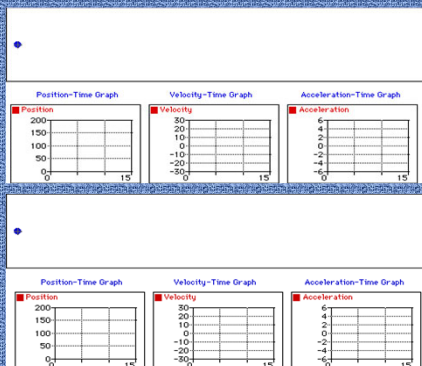
**Motion Diagrams and Graphs**  
**constant acceleration**



PHYS 21: Chap. 2, Pg 24

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## Motion Diagrams and Graphs constant acceleration



Chapter 2, Pg 25

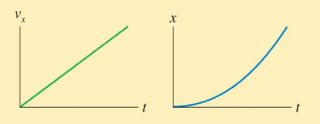
25

## 1D Kinematics (including free fall)

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### Motion with constant acceleration

An object with constant acceleration has a constantly changing velocity. Its velocity graph is linear; its position graph is a parabola.



Kinematic equations for motion with constant acceleration:

$$a = \frac{\Delta v}{\Delta t}$$

$$(v_x)_f = (v_x)_i + a_x \Delta t$$

$$v(t)$$

$$v = \frac{\Delta x}{\Delta t}$$

$$x_f = x_i + (v_x)_i \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$x(t)$$

$$(v_x)_f^2 = (v_x)_i^2 + 2a_x \Delta x$$

$$v(x)$$

Chapter 2, Pg 27

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### SYNTHESIS 2.1 Describing motion in one dimension

We describe motion in terms of position, velocity, and acceleration.

#### For all motion:

Velocity is the rate of change of position, in m/s.  $v_x = \frac{\Delta x}{\Delta t}$   
Acceleration is the rate of change of velocity, in m/s<sup>2</sup>.  $a_x = \frac{\Delta v_x}{\Delta t}$

#### For uniform motion:

• acceleration is zero  
• velocity is constant  
• position changes steadily

The velocity is constant, so the slope of the position graph is constant as well.  
The slope is  $v_x$ .  
Final and initial position (m)  
 $x_f = x_i + v_x \Delta t$  (2.4)  
Velocity (m/s)  
Time interval (s)

#### For motion with constant acceleration:

• acceleration is steady; it does not change  
The acceleration is constant, so the slope of the velocity graph is constant.

The velocity steadily increases, so the slope of the position graph steadily increases.  
The slope is  $a_x$ .

• velocity changes steadily

Final and initial velocity (m/s)  
 $(v_x)_f = (v_x)_i + a_x \Delta t$  (2.11)  
Acceleration (m/s<sup>2</sup>)  
Time interval (s)

• the position changes as the square of the time interval  
The velocity steadily increases, so the slope of the position graph steadily increases.

This gives us a third equation, which is useful for many kinematics problems.

Final and initial position (m)  
 $x_f = x_i + (v_x)_i \Delta t + \frac{1}{2} a_x (\Delta t)^2$  (2.12)  
Initial velocity (m/s)  
Acceleration (m/s<sup>2</sup>)  
Time interval (s)

• we can also express the change in velocity in terms of displacement, not time

Final and initial velocity (m/s)  
 $(v_x)_f^2 = (v_x)_i^2 + 2a_x \Delta x$  (2.13)  
Acceleration (m/s<sup>2</sup>)  
Change in position (m)

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### ConceptTest 2

### Kinematics

If the velocity of an object is non-zero ( $v \neq 0$ ), can the acceleration of the object be zero?

1. yes
2. no
3. depends on the velocity

Follow-up: How about the other way around?

Can an object have a non-zero acceleration, but zero velocity?

0 of 5

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### ConceptTest 4

### Kinematics

If the velocity of an object is zero ( $v = 0$ ), can the acceleration of the object be non-zero ( $a \neq 0$ )?

1. yes
2. no
3. depends on the velocity

0 of 5

Part 10, Chap. 1, Pg 28

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Give a specific example for each of the following situations:

1)  $a = 0$  but  $v \neq 0$

2)  $v = 0$  but  $a \neq 0$

3)  $v < 0$  and  $a > 0$

2.15

PHYS 21: Chap. 2, Pg 31

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Indicate whether the quantities in the table are positive (+), negative (-) or zero (0).



**C**

**D**

	A	B	C	D
initial position				
final position				
initial velocity				
final velocity				
accel.				

1.30 PHYS 21: Chap. 2, Pg 32

32

Indicate whether the quantities in the table are positive (+), negative (-) or zero (0).



**C**

**D**

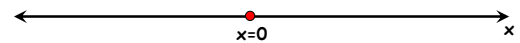
	A	B	C	D
initial position	0	0	0	+
final position	+	-	+	0
initial velocity	+	0	0	-
final velocity	0	-	+	-
accel.	-	-	+	-

PHYS 21: Chap. 2, Pg 33

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The kinematic variables for position, velocity and acceleration have 8 possible combinations of signs, such as  $(x, v, a) = (+, -, +)$  for example.

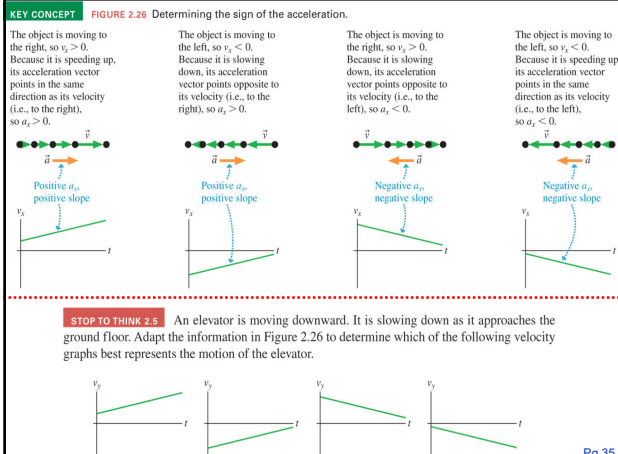
List all 8 combinations. Draw a motion diagram for each case and draw the corresponding velocity and acceleration vectors.



1.31

PHYS 21: Chap. 2, Pg 34

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Pg 35

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A truck driver has a shipment of apples to deliver to a store 500 miles away. The trip usually takes him 8 hours. Today he is daydreaming and realizes 150 miles into his trip that he is running a half hour later than his usual pace at this point.

How fast must he drive for the remainder of the trip in order to complete the trip in the usual amount of time?

$v = 68.6 \text{ mph}$

3+2=5  
2.57

PHYS 21: Chap. 2, Pg 36

36

A truck driver has a shipment of apples to deliver to a store 500 miles away. The trip usually takes him 8 hours. Today he is daydreaming and realizes 150 miles into his trip that he is running a half hour later than his usual pace at this point.

How fast must he drive for the remainder of the trip in order to complete the trip in the usual amount of time?

$$v_{avg} = \frac{500 \text{ miles}}{8 \text{ hrs}} = 62.5 \frac{\text{miles}}{\text{hr}} \quad v = 68.6 \text{ mph}$$

Normally:  $t_1 = \frac{150 \text{ miles}}{62.5 \text{ mph}} = 2.4 \text{ hrs}$   $t_2 = \frac{350 \text{ miles}}{62.5 \text{ mph}} = 5.6 \text{ hrs}$

But today:  $t_1 = 2.9 \text{ hrs}$   $t_2 = 5.1 \text{ hrs}$

So to make up lost time:  $v_{fast} = \frac{350 \text{ miles}}{5.1 \text{ hrs}} = 68.6 \frac{\text{miles}}{\text{hr}}$

PHYS 21: Chap. 2, Pg 37

37

A truck driver has a shipment of apples to deliver to a store 500 miles away. The trip usually takes him 8 hours. Today he is daydreaming and realizes halfway into his trip (at the 250 mile mark) that he is running a half hour later than his usual pace at this point.

How fast must he drive for the remainder of the trip in order to complete the trip in the usual amount of time?

$$v = 71.4 \text{ mph}$$

2.57

PHYS 21: Chap. 2, Pg 38

38

A truck driver has a shipment of apples to deliver to a store 500 miles away. The trip usually takes him 8 hours. Today he is daydreaming and realizes halfway into his trip (at the 250 mile mark) that he is running a half hour later than his usual pace at this point.

How fast must he drive for the remainder of the trip in order to complete the trip in the usual amount of time?

$$v_{avg} = \frac{500 \text{ miles}}{8 \text{ hrs}} = 62.5 \frac{\text{miles}}{\text{hr}} \quad v = 71.4 \text{ mph}$$

Normally each half of the trip requires:  $t_1 = t_2 = \frac{250 \text{ miles}}{62.5 \text{ mph}} = 4 \text{ hrs}$

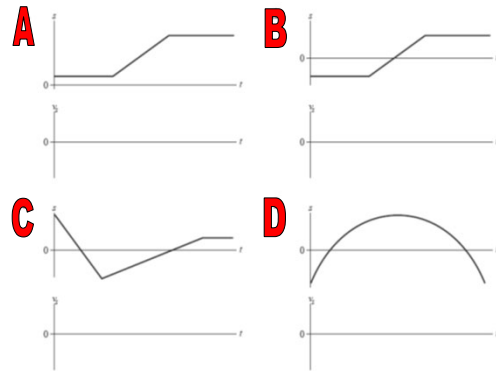
But today:  $t_1 = 4.5 \text{ hrs}$   $t_2 = 3.5 \text{ hrs}$

So to make up lost time:  $v_{fast} = \frac{250 \text{ miles}}{3.5 \text{ hrs}} = 71.4 \frac{\text{miles}}{\text{hr}}$

PHYS 21: Chap. 2, Pg 39

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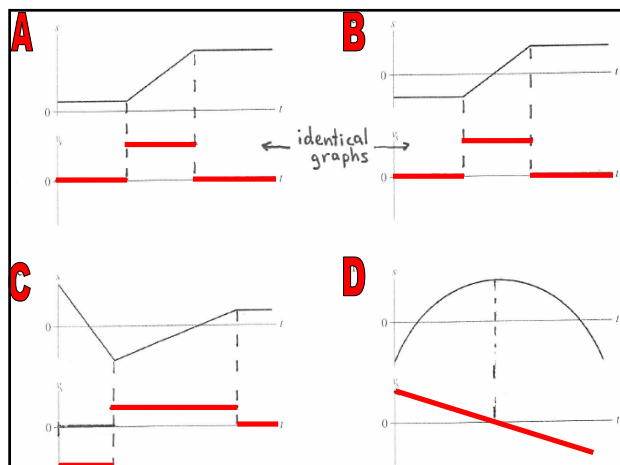
For the  $x$  vs.  $t$  graphs, draw corresponding  $v$  vs.  $t$  graphs.



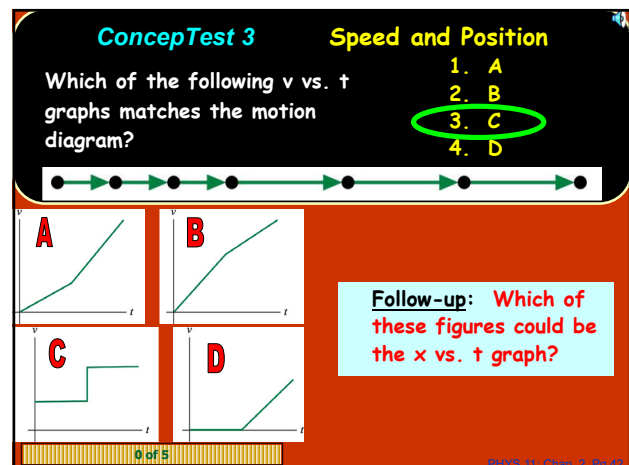
2.7

PHYS 21: Chap. 2, Pg 40

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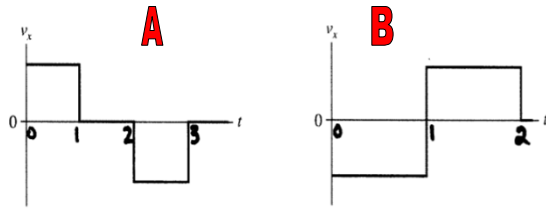
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For the  $v$  vs.  $t$  graphs, draw corresponding  $x$  vs.  $t$  graphs. Describe the motion in words. Assume that  $x_0 = 0$ .

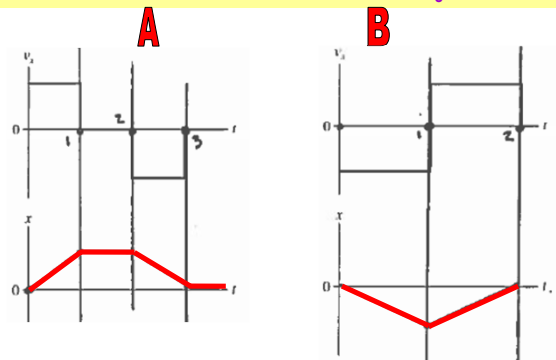


2.8

PHYS 21: Chap. 2, Pg 43

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For the  $v$  vs.  $t$  graphs, draw corresponding  $x$  vs.  $t$  graphs. Describe the motion in words. Assume that  $x_0 = 0$ .



2.8

PHYS 21: Chap. 2, Pg 44

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